





## Separating dynamics, physics and tracer transport grids in a global climate model

## **Peter Hjort Lauritzen**

Atmospheric Modeling and Predictability Section Climate and Global Dynamics Laboratory National Center for Atmospheric Research

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### Why?





## **Cost per additional tracer** (dynamical core timings using 1728 tasks)

#### 1 degree horizontal resolution, 30 levels



## The terminator 'toy'-chemistry test: A simple tool to assess errors in transport schemes

(Lauritzen et al., 2015) See: <u>http://www.cgd.ucar.edu/cms/pel/terminator.html</u>

• Consider 2 reactive chemical species, Cl and Cl<sub>2</sub>:

$$Cl_2 \rightarrow Cl + Cl : k_1$$
$$Cl + Cl \rightarrow Cl_2 : k_2$$

• Steady-state solution (no flow):



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• In any flow-field Cl<sub>y</sub>=Cl+2\*Cl<sub>2</sub> should be constant at all times (correlation preservation)





Terminator reaction coefficient:  $k_1(\lambda, \theta)$ 



## The terminator 'toy'-chemistry test: A simple tool to assess errors in transport schemes

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90°N



5.00e-6 4.30e-6 45°N -4.10e-6 4.03e-6 4.01e-6 0° -3.99e-6 3.97e-6 3.90e-6 45°S -3.70e-6 3.00e-6 90°S -180° 90°W 0° 90°E 180° Day 00 **CAM-FV (Lin 2004)** 90°N 5.00e-6 4.30e-6 45°N 4.10e-6 4.03e-6 4.01e-6 0° 3.99e-6 3.97e-6 3.90e-6 45°S 3.70e-6 CL 3.00e-6 90°S -90°W 0° 180° 90°E 180° **Dav 00** 

**CAM-SE** 

Errors are due to non-conservation of linear correlations in tracer transport scheme and/or physics-dynamics coupling

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## **Problem formulation**

## **Improve the efficiency and accuracy of tracer transport in CAM-SE**



Note: It is easy to make an efficient model that is inaccurate or an accurate model that is inefficient (at least for smooth problems) ...

## **Tracer transport: Continuity equation**

Consider the continuity equation of air mass (pressure level thickness  $\Delta p$ ), and tracer mass ( $\Delta pq$ , where q mixing ratio)

$$\frac{\partial \psi}{\partial t} + \nabla \cdot (\psi \vec{v}) = 0, \qquad \psi = \Delta p, \Delta pq,$$

No sources/sinks

respectively, where  $\vec{v}$  wind vector.



# **Requirements for transport schemes intended for global climate/climate-chemistry applications:**

#### 1. Global (and local) Mass-conservation

The solution to the continuity equation without sources/sinks must conserve mass. Very important!

#### 2. Physical realizable solutions (shape-preservation)

Scheme must not produce new extrema (in particular negatives) in q



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# **Requirements for transport schemes intended for global climate/climate-chemistry applications:**

3. Preservation of functional relations between tracers

Transport scheme preserves  $q_2 = f(q_1)$ 



Figure: Aircraft observations of long-lived species in the stratosphere

Tracer transport scheme should not unphysically perturb these relations between tracers

# **Requirements for transport schemes intended for global climate/climate-chemistry applications:**

4. Consistency (tracer and air mass are coupled!)

Continuity equations for air mass and tracer mass:

$$\frac{\partial (\Delta p)}{\partial t} + \nabla \cdot (\Delta p \vec{v}) = 0, \qquad (1)$$

$$\frac{\partial (\Delta pq)}{\partial t} + \nabla \cdot (\Delta p q \vec{v}) = 0, \qquad (2)$$

If q = 1 then the transport scheme should reduce to the continuity equation for air.

#### In model consistency is non-trivial if:

- Using prescribed wind and mass fields from , e.g., re-analysis.
- (2) is solved with a different numerical method than (1)



Basic formulation

Lauritzen et al. (2010)

### Conservative Semi-LAgrangian Multi-tracer (CSLAM)



Finite-volume Lagrangian form of continuity equation for air (pressure level thickness,  $\Delta p$ ), and tracer (mixing ratio, q):

$$\int_{A_k} \psi_k^{n+1} dA = \int_{a_k} \psi_k^n dA = \sum_{\ell=1}^{L_k} \left[ \int_{a_{k\ell}} \psi_{k\ell}^n(x,y) dA \right], \quad \psi = \Delta p, \, \Delta p \, q,$$

where *n* time-level,  $a_{k\ell}$  overlap areas,  $L_k$  #overlap areas, and  $\psi_{k\ell}^n(x, y)$  reconstruction function in cell  $k\ell$ .



Basic formulation

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Basic formulation

Lauritzen et al. (2010)

### Conservative Semi-LAgrangian Multi-tracer (CSLAM)



- Multi-tracer efficient:  $w_{k\ell}^{(i,j)}$  re-used for each additional tracer (Dukowicz and Baumgardner, 2000).
- Scheme allows for large time-steps (flow deformation limited).
- Conserves mass, shape, linear correlations (Lauritzen et al., 2014).



Basic formulation

Lauritzen et al. (2010)

## Conservative Semi-LAgrangian Multi-tracer (CSLAM)

#### Shape-preservation

• Apply limiter to mixing ratio sub-grid cell distribution:

$$q(x,y) = \sum_{i+j<3} c^{(i,j)} x^i y^j,$$

(Barth and Jespersen, 1989) so that extrema of q(x, y) are within range of neighboring  $\overline{q}$ .



## **Extension to cubed-sphere:** Figure shows upstream Lagrangian grid







Basic formulation

Harris et al. (2010)

### Flux-form CSLAM = Lagrangian CSLAM



$$\int_{A_k} \psi_k^{n+1} \, dA = \int_{A_k} \psi_k^n \, dA - \sum_{\epsilon=1}^4 s_{k\ell}^\epsilon \int_{a_k^\epsilon} \psi \, dA, \quad \psi = \Delta p, \, \Delta p \, q.$$

where

- $a_k^{\epsilon} = \text{`flux-area'} (\text{yellow area}) = \text{area swept through face } \epsilon$
- $s_{k\ell}^{\epsilon} = 1$  for outflow and -1 for inflow.

Flux-form and Lagrangian forms of CSLAM are equivalent (Lauritzen et al., 2011).



## Coupling finite-volume semi-Lagrangian transport with spectral element dynamics

4. Consistency (tracer and air mass are coupled!)

Continuity equations for air mass and tracer mass:

**Spectral elements** 

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**CSLAM** 

$$\frac{\partial (\Delta p)}{\partial t} + \nabla \cdot (\Delta p \vec{v}) = 0,$$
$$\int_{A_k} (\Delta p q)_k^{n+1} dA = \int_{a_k} (\Delta p q)^n dA.$$

If q = 1 then the transport scheme should reduce to the continuity equation for air.

We need to couple without violating mass-conservation, shape-preservation, and consistency



Continuity equation for  $\Delta p$ :

$$\frac{\partial \Delta p}{\partial t} = -\nabla \cdot \Delta p \vec{v} + \tau \nabla^4 \Delta p.$$



Continuity equation for  $\Delta p$ :

$$\left\langle h_k, \frac{\partial \Delta p}{\partial t} \right\rangle = \left\langle h_k, -\nabla \cdot \Delta p \vec{v} \right\rangle + \left\langle h_k, \tau \nabla^4 \Delta p \right\rangle,$$

where  $\langle h_k, \cdot \rangle$  is inner product

$$\langle h_k, f \rangle = \sum_{i,j} w_{i,j} h_k(x_i, y_j) f(x_i, y_j) \sim \iint h_k f \, dA.$$



Continuity equation for  $\Delta p$ :

$$\left\langle h_k, \frac{\Delta p^* - \Delta p^n}{\Delta t} \right\rangle = \left\langle h_k, -\nabla \cdot \Delta p \vec{v} \right\rangle + \left\langle h_k, \tau \nabla^4 \Delta p \right\rangle.$$



Projection step

$$\Delta p^{n+1} = DSS\left(\Delta p^*\right)$$

where *DSS* refers to *Direct Stiffness Summation* (also referred to as assembly or inverse mass matrix step).

 Choice of GLL quadrature based inner product and nodal basis functions gives a diagonal mass matrix (Maday and Patera, 1987).



Continuity equation for  $\Delta p$ :

$$\left(h_k, \frac{\Delta p^{n+1} - \Delta p^n}{\Delta t}\right) = \left\langle h_k, -\nabla \cdot \Delta p \vec{v} \right\rangle + \left\langle h_k, \tau \nabla^4 \Delta p \right\rangle + \left\langle h_k, D \right\rangle.$$



Continuity equation for  $\Delta p$ :

$$\left(h_k,\frac{\Delta p^{n+1}-\Delta p^n}{\Delta t}\right)=\left\langle h_k,F\right\rangle+\left\langle h_k,G\right\rangle+\left\langle h_k,D\right\rangle.$$



### **Diagnosing fluxes from spectral-element method**

• There exist a basis  $\phi_k$  so that

$$\left(\phi_k, \frac{\Delta p^{n+1} - \Delta p^n}{\Delta t}\right) = \left\langle\phi_k, F\right\rangle + \left\langle\phi_k, G\right\rangle + \left\langle\phi_k, D\right\rangle,$$

gives the change of mass in each CSLAM control volume.

 Moreover, each term on right-hand side can be expressed in terms of edge fluxes:

$$\left(\Delta p^{n+1} - \Delta p^n\right) \Delta A_k = \sum_{\epsilon=1}^4 \left[\mathcal{F}_F^{(\epsilon)} + \mathcal{F}_G^{(\epsilon)} + \mathcal{F}_D^{(\epsilon)}\right].$$



## The story so far

#### **Spectral-Element Method: CAM-SE**

Mass change over CSLAM control volume  $A_k$  implied by SE

$$\left(\Delta p^{n+1} - \Delta p^n\right)\Delta A_k = \sum_{\epsilon=1}^4 \left[\mathcal{F}_F^{(\epsilon)} + \mathcal{F}_G^{(\epsilon)} + \mathcal{F}_D^{(\epsilon)}\right],$$

(Lauritzen et al., 2016; in prep).

#### **Finite-Volume Method: CSLAM**



CSLAM discretization is given by

$$\left(\widetilde{\Delta p}^{n+1} - \widetilde{\Delta p}^n\right) \Delta A_k = \sum_{\epsilon=1}^4 \left[\mathcal{F}_{CSLAM}^{(\epsilon)}\right] = -\sum_{\epsilon=1}^4 s_{k\ell}^{\epsilon} \int_{a_k^{\epsilon}} \Delta p^n \, dA.$$

Lauritzen et al., (2011)

## The story so far

#### **Spectral-Element Method: CAM-SE**

Mass change over CSLAM control volume  $A_k$  implied by SE



## Consistent SE-CSLAM algorithm: step-by-step example



Well-posed? As long as flow deformation  $\left|\frac{\partial u}{\partial x}\right| \Delta t \lesssim 1$  (Lipschitz criterion)

Lauritzen et al., 2016

### Consistent SE-CSLAM algorithm: step-by-step example

Local iteration problem generating an upstream grid that spans the sphere without cracks and overlaps

=> all CSLAM technology from Lauritzen et al. (2010) can be used



Well-posed? As long as flow deformation  $\left|\frac{\partial u}{\partial x}\right| \Delta t \lesssim 1$  (Lipschitz criterion)

## **Consistent CSLAM algorithm is general**

In principle, the consistent CSLAM algorithm can be made consistent with any fluxes that obey the Lipschitz criterion ...





## **Idealized baroclinic wave test**

No sub-grid-scale forcing, dry, balanced initial condition with perturbation Jablonowski and Williamson (2006)

**Surface pressure computed with CSLAM is identical to SE (to round-off)** 

## **3 tracers: initial conditions**






### CAM-SE-CSLAM

### **CAM-SE reference**





### **CAM-SE**

**CAM-SE-CSLAM** 

### **CAM-SE reference**



### **CAM-SE**

**CAM-SE-CSLAM** 

### **CAM-SE reference**



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Terminator reaction coefficient:  $k_1(\lambda, \theta)$ 



## **Initial condition**



## **CAM-SE**





day 9



## **CAM-SE-CSLAM**



## Performance



- All simulations run on NCAR's Yellowstone computer
- No exploration of threading



## **MPI communication**



For every 30 minute physics time-step:

- SE performs 6 tracer time-steps (dt=300s)
- CSLAM performs 2 tracer time-steps (dt=900s) => 2 MPI calls (1 per tracer dt)

=> 42 MPI calls (7 per tracer dt)

That said, CSLAM needs a much larger halo than SE:





### **Performance**



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### **Performance: strong scaling**



**Fracer transport** [s]

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### How do we compare with CAM-FV (dynamical core timings using 1728 tasks)

1 degree horizontal resolution, 30 levels



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### How do we compare with CAM-FV (dynamical core timings using 1728 tasks)

### 1 degree horizontal resolution, 30 levels



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### **Performance: break-down of CSLAM algorithm**



Number of tracers

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# **Part II: Coupling to physics**

There are several reasons why I do not think one should pass state on GLL points to physics:





## Non-uniform sampling of atmospheric state

Current physics/"coupler" grid

Gets worse with increasing order!













## Aside

# A couple of comments on topography generation and topography smoothing



### Geoscientific Model Development In interactive open-access journal of the European Geos Geosci. Model Dev., 8, 3975-3986, 2015 http://www.geosci-model-dev.net/8/3975/2015/ doi:10.5194/gmd-8-3975-2015 Volume 8, issue 12 O Copernicus Publication © Author(s) 2015. This work is distributed Related article der the Creative Commons Attribution 3.0 License. Model description paper 14 Dec 2015 ÷ 0 NCAR\_Topo (v1.0): NCAR global model topography generation software for unstructured grids P. H. Lauritzen<sup>1</sup>, J. T. Bacmeister<sup>1</sup>, P. F. Callaghan<sup>1</sup>, and M. A. Taylor </> nal Center for Atmospheric Research, 1850 Table Mesa Drive, Boulder, Colorado, USA Sandia National Laboratories, Albuquerque, New Mexico, USA Received: 12 May 2015 - Published in Geosci. Model Dev. Discuss.: 22 Jun 2015 Revised: 30 Sep 2015 - Accepted: 01 Dec 2015 - Published: 14 Dec 2015 his paper documents the NCAR global model topography generation software. The software Abstract. It is the purpose of this paper to document the NCAR global model topography generation software for unstructured grid: (NCAR\_Topo (v1.0)). Given a model grid, the software computes the fraction of the grid box covered by land, the grid-box mean penerates... Read more elevation (deviation from a peoid that defines nominal sea level surface), and associated sub-orid-scale variances commonly used for gravity wave and turbulent mountain stress parameterizations. The software supports regular latitude-longitude grids as well as Citation BibTeX unstructured grids, e.g., icosahedral, Voronoi, cubed-sphere and variable-resolution grids. EndNote

Citation: Lauritzen, P. H., Bacmeister, J. T., Callaghan, P. F., and Taylor, M. A.: NCAR\_Topo (v1.0): NCAR global model topography generation software for unstructured grids, Geosci. Model Dev., 8, 3975-3986, doi:10.5194/gmd-8-3975-2015, 2015.



(GMTED2010)

GTOPO30: USGS ~1km dataset from 1996 **Global Multi-resolution Terrain Elevation Data 2010 GMTED2010**)

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USGS 30sec (~

variables:

GMTED2010 is based on data derived from 11 rasterbased elevation sources. The primary source dataset for GMTED2010 is NGA's SRTM Digital Terrain Elevation Data (DTED<sup>®</sup>2, *http://www2.jpl.nasa.gov/srtm/*) (void-filled) 1-arc-second data. For the geographic areas outside the SRTM coverage area and to fill in remaining holes in the SRTM data, the following sources were used: (1) non-SRTM DTED<sup>®</sup>, (2) Canadian Digital Elevation Data (CDED) at two resolutions, (3) Satellite Pour l'Observation de la Terre (SPOT 5) Reference3D, (4) National Elevation Dataset (NED) for the continental United States and Alaska, (5) GEODATA 9 second digital elevation model (DEM) for Australia, (6) an Antarctica satellite radar and laser altimeter DEM, and (7) a Greenland (height : LANDFRAC satellite radar altimeter DEM. Each is described below. (land fra

## Elevation differences [meters]

(on 3km cubed-sphere grid)





### Elevation power spectra



# Topography smoothing in CAM

### WARNING: CAM-HOMME (with Eulerian vertical advection) i.e. results NOT CAM-SE (with Lagrangian vertical coordinate)

### 30 year AMIP simulations



OMEGA, JJA, model level 16 (approximately 323 hPa)

Notation: 2.5xdiv =  $2.5^2$  times more divergence damping than vorticity damping 4x, 8x, ..., 32x = smoothing of surface geopotential height

# Topography smoothing in CAM

WARNING: CAM-HOMME (with Eulerian vertical advection) i.e. results NOT CAM-SE (with Lagrangian vertical coordinate)

30 year AMIP simulations



Mean sea level pressure differences, DJF, diff

Lauritzen et al., (2015): NCAR Global Model Topography Generation Software for Unstructured Grids





## **Grid-scale forcing**



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## Held-Suarez with topography



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## **CAM-SE-CSLAM with moisture**

"This is where the fun begins!" – Staniforth et al. (2006)







## Mapping u,v, T, omega from dynamics grid (GLL) to finite-volume (CSLAM) grid

Temperature: Integrate basis function representation of dp\*T over physics grid control volumes (high-order remapping; conserves dry internal energy)







## **CAM-SE-CSLAM configuration**



# **Temperature tendency: FT**

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### CAM-SE-CSLAM with linear interpolation from phys to dyn: 5 month average

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## **PRECT** (TOTAL PRECIPITATION RATE)



### CAM4 SE-CSLAM-physgrid: linear interpolation phys to dyn: 5 month average

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# **Temperature tendency: FT**



### CAM-SE-CSLAM with cubic tensor product interpolation from phys to dyn: 18 month average

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## **PRECT** (TOTAL PRECIPITATION RATE)



CAM-SE-CSLAM with cubic tensor product interpolation from phys to dyn: 18 month average

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## Held-Suarez with topography



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## Held-Suarez with topography





## **Uniform sampling of atmospheric state**



Figure courtesy of A. Herrington





## **CAM-SE-physgrid**

**Capability to run physics** on 2x2,3x3,4x4,... grids u,v,T,p Lander and Hoskins (1997): only pass physics "believable" scales to physics! **Coarser physics grid Finer physics grid** 



- Presented algorithm to consistently couple spectral-element dynamics with remap finite-volume transport
- Accuracy is improved for "non-smooth" tracer distributions when using CAM-SE-CSLAM compared to CAM-SE.
- Note that our modeling framework is quite unique in the sense that we support finite-volume and high-order Galerkin methods in the same framework
- Capability to run physics on different grid than dynamics
- CAM-SE physgrid and CAM-SE-CSLAM (uses physgrid) are scheduled to be released with CESM2 later this year



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0 More information: <u>http://www.cgd.ucar.edu/cms/pel</u> Email: pel@ucar.edu NCAR | National Center for Atmospheric Research UCAR | Climate & Global Dynamics